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NUMERICAL SOLUTION OF THERMO-DIFFUSION AND DIFFUSION-THERMO EFFECTS ON UNSTEADY MHD FREE CONVECTIVE MASS TRANSFER FLOW PAST AN INFINITE VERTICAL POROUS PLATE WITH OSCILLATORY SUCTION VELOCITY

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Abstract

Diffusion Thermo(Dufour) and thermal diffusion(Soret) effects on free convection and mass transfer unsteady magnetohydrodynamic flow of an electrically conducting viscous incompressible fluid past an infinite vertical porous plate under oscillatory suction velocity. The problem is solved numerically by using finite element method for velocity, temperature and concentration field and also the expression for skin friction, rate of heat and mass transfer have been obtained. The results obtained have been presented numerically through graphs and tables for externally cooled plate (Gr > 0) and externally heated plate (Gr < 0) to observe the effects of various parameters encountered in the equations.

Key words: Mass transfer, MHD flow, vertical plate, suction velocity, Soret and Dufour numbers, finite element method.

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1. INTRODUCTION:

The problem of unsteady MHD free convective mass transfer flow past an infinite vertical porous plate with oscillatory suction velocity in presence of soret and dufour has attracted the interest of many researchers in view of its applications related to geophysical, petrochemical and chemical engineering. When heat and mass transfer occur simultaneously between the fluxes the driving potentials are of more intricate nature. An energy flux can be generated not only by temperature gradients but by composition gradients as well. The energy flux caused by a composition is called Dufour or diffusion-thermo effect. Temperature gradients can also create mass fluxes, and this is the Soret or thermal-diffusion effect. Generally, the thermal-diffusion and the diffusion-thermo effects are of smaller order magnitude than the effects prescribed by Fourier's or Fick's laws and are often neglected in heat and mass transfer processes. These effects are considered as second order phenomena and may become significant in areas such as hydrology, petrology, geosciences, etc.

The study of radiative heat and mass transfer in convective flows is important from many industrial and technological points of view. Mass transfer is one of the most commonly encountered phenomenon in chemical industries as well as in physical and biological sciences. When mass transfer takes place in a fluid at rest, the mass is transferred purely by molecular diffusion resulting from concentration gradients. For low concentration of the mass in the fluid and low mass transfer rates, the convective heat and mass transfer process are similar in nature. A number of investigations have already been carried out with combined heat and mass transfer under the assumption of different physical situations.

In recent years, progress has been considerably made in the study of heat and mass transfer in MHD flows due to its application in many devices, like the MHD power generators and Hall accelerators. Magneto hydrodynamic free convection finds applications in fluid engineering problems such as MHD pumps, accelerators and flow meters, plasma studies, nuclear reactors, geothermal energy extraction, *etc.* R. Srinivasa Raju et. al [2016] discussed the Analytical and Numerical study of unsteady MHD free convection flow over an exponentially moving vertical plate with Heat Absorption. Pal and Talukdar (2009) analyzed the combined effect of mixed convection with thermal radiation and chemical reaction on MHD flow of viscous and electrically conducting fluid past a vertical permeable surface embedded in a porous medium is analyzed. Asma Khalid et. al, [2015] studied the Unsteady MHD free convection flow of Casson fluid past over an oscillating vertical plate embedded in a porous medium. Md Alamgir Kabir and Md Abdullah Al Mahbub [2012] discussed the Effects of Thermophoresis on Unsteady MHD Free Convective Heat and Mass Transfer along an Inclined Porous Plate with Heat Generation in Presence of Magnetic Field. V. S. Rao et. al., [2013] analyzed the effect of Radiation and Mass Transfer Flow Past Semi-Infinite Moving Vertical Plate with Viscous Dissipation. Hayat *et al.* (2010) analyzed a mathematical model in order to study the heat and mass transfer characteristics in mixed convection boundary layer flow about a linearly stretching vertical surface in a porous medium filled with a viscoelastic fluid, by taking into account the diffusion thermo (Dufour) and thermal-diffusion (Soret) effects. N. Vedavathi et. al [2015] analyzed the Radiation and mass transfer effects on unsteady MHD convective flow past an infinite vertical plate with Dufour and Soret effects.

Ming-chun *et al.* (2006) took an account of the thermal diffusion and diffusion-thermo effects, to study the properties of the heat and mass transfer in a strongly endothermic chemical reaction system for a porous medium. Gaikwad *et al.* (2007) investigated the onset of double diffusive convection in a two component couple of stress fluid layer with Soret and Dufour effects using both linear and non-linear stability analysis. Osalusi *et al.* (2008) investigated thermo-diffusion and diffusion-thermo effects on combined heat and mass transfer of a steady hydromagnetic convective and slip flow due to a rotating disk in the presence of viscous dissipation and Ohmic heating. Shateyi (2008) investigated thermal radiation and buoyancy effects on heat and mass transfer over a semi-infinite stretching surface with suction and blowing.

The interaction of buoyancy with thermal radiation has increased greatly during the last decade due to its importance in many practical applications. The thermal radiation effect is important under many isothermal and non isothermal situations. If the entire system involving the polymer extrusion process is placed in a thermally controlled environment, then thermal radiation could be important. The knowledge of radiation heat transfer in the system can, perhaps, lead to desired product with sought characteristics. Motsa (2008) investigated the effect of both the Soret and Dufour effects on the onset of double diffusive

convection. Mansour *et al.* (2008) investigated the effects of chemical reaction, thermal stratification, Soret and Dufour number on MHD free convective heat and mass transfer of a

viscous, incompressible and electrically conducting fluid on a vertical stretching surface embedded in a saturated porous medium. Srihari *et al.* (2006) studied the Soret effect on unsteady MHD free convective mass transfer flow past an infinite vertical porous plate with oscillatory suction velocity and heat sink. P V S N Murthy *et al.* (2010) discussed the Soret and Dufour Effects on Free Convection Heat and Mass Transfer from a Horizontal Flat Plate in a non-Darcy Porous Medium.

D.Srinivasacharya and Ch. RamReddy (2011) studied the Soret and Dufour effects on mixed convection from an exponentially stretching surface. M. Narayana *et al.*(2013) studied the Soret effect on the natural convection from a vertical plate in a thermally stratified porous medium saturated with non-Newtonian liquid. Srinivasacharya D and Kaladhar K (2014) investigated the Mixed convection flow of chemically reacting Couple stress fluid in a vertical channel with Soret and Dufour effects.

In view of the imporatance of thermal difusion and difussion thermo effects and the numerous possible industrial applications of the problem (like in isotope seperation), it is of paramount interest in this study to investigate the effects of Soret and Dufour on unsteady MHD free convective mass transfer flow past an infinite vertical porous plate with oscillatory suction velocity. None of the above investigations simultaneously studied the effects of Soret and Dufour on unsteady MHD free convective mass transfer flow past an infinite vertical porous plate with oscillatory suction velocity. Hence, the purpose of this paper is to extend Srihari (2006), to study the more general problem which include Soret and Dufour effects on unsteady MHD free convective mass transfer flow past an infinite vertical porous plate with oscillatory suction velocity. In this study the effects of different flow parameters encountered in the equations were also studied. The problem is solved numerically by using finite element method, which is more economical from computational view point.

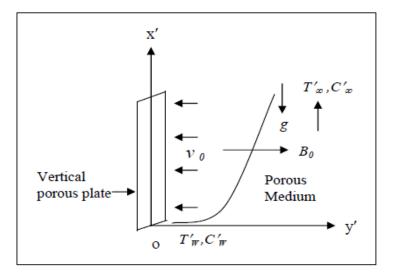


Figure A. Physical sketch and geometry of the problem

2. MATHEMATICAL FORMULATION:

We consider the unsteady hydro magnetic flow of an incompressible, electrically conducting viscous fluid through porous medium, past an infinite vertical plate with oscillatory suction. In Cartesian co-ordinate system, x'-axis is assumed to be along plate in the direction of the flow and y'-axis normal to it. A normal magnetic field is assumed to be applied in y' – direction and the induced magnetic field is negligible in comparison with the applied one which corresponds to very small magnetic Reynolds number. The surface is maintained at uniform constant temperature and concentration. The flow has significant Thermal Radiation, Soret and Dufour effects. Under the stated assumptions and taking the usual Boussinesq's approximation in to account.

The governing equations for momentum, energy and concentration in dimensionless form are:

$$\frac{1}{4}\frac{\partial u}{\partial t} - \left(1 + \varepsilon e^{\operatorname{int}}\right)\frac{\partial u}{\partial y} = Gr T + GmC + \frac{\partial^2 u}{\partial y^2} - \frac{u}{K_o\left(1 + \varepsilon e^{\operatorname{int}}\right)} - M^2 u \tag{1}$$

$$\frac{1}{4}\frac{\partial T}{\partial t} - (1 + \varepsilon e^{int})\frac{\partial T}{\partial y} = \frac{1}{\Pr}\frac{\partial^2 T}{\partial y^2} + Du\left(\frac{\partial^2 C}{\partial y^2}\right)$$
(2)

$$\frac{1}{4}\frac{\partial C}{\partial t} - (1 + \varepsilon e^{int})\frac{\partial C}{\partial y} = \frac{1}{Sc}\frac{\partial^2 C}{\partial y^2} + So\left(\frac{\partial^2 T}{\partial y^2}\right)$$
(3)

$$u = 0, T = 1 + \varepsilon e^{int}, C = 1 + \varepsilon e^{int} at y = 0$$

$$u \to 0, T \to 0, C \to 0, as y \to \infty (4)$$

The non-dimensionless quantities introduced in these equations are defined as:

$$y = \frac{v_o y'}{4v}; t = \frac{v_o^2 t'}{4v}; \eta = \frac{49\eta'}{v_o^2}; u = \frac{u'}{v_o}; T = \frac{T' - T_\infty}{T_w - T_\infty}; C = \frac{C' - C_\infty}{C_w - C_\infty};$$

$$K_o = \frac{K'_o v_o^2}{9^2} (Cons \tan t \ permeability \ of \ the \ medium);$$

$$So = \frac{D_1(T_w - T_\infty)}{9(C_w - C_\infty)} (Soret \ number); Du = \frac{D_1(C_w - C_\infty)}{9(T_w - T_\infty)} (Dufour \ number);$$

$$Gr = \frac{9g\beta^*(T_w - T_\infty)}{v_o^3} (Grashof \ Number); Sc = \frac{9}{D_1} (Schimidt \ Number);$$

$$\Pr = \frac{\mu C_p}{K_t} (\Pr \ andtl \ Number); M = \frac{B_o}{v_o} \sqrt{\frac{\sigma 9}{\rho}} (Magnetic \ Parameter) \ and$$

$$Gm = \frac{9g\beta(C_w - C_\infty)}{v_o^3} (Modofied \ Grashof \ Number).$$

Where u is the velocity along the x-axis, ρ is the density of the fluid, ϑ is the kinematic coefficient of viscosity, η is the frequency of oscillation, g is the acceleration due to gravity, t is the time, β is the coefficient of volume expansion for the heat transfer, β^* is the volumetric coefficient of expansion with species concentration, T is the fluid temperature, T_{∞} is the fluid temperature at infinity, C is the species concentration, C_{∞} is the species concentration at infinity, D₁ is the chemical molecular diffusivity, Ko is the constant permeability of the medium, μ is the coefficient of viscosity, Cp is the specific heat at constant pressure.

3. METHOD OF SOLUTION:

The Galerkin equation for the differential equation (1) becomes

$$\int_{y_j}^{y_k} \left\{ N^T \left[\frac{\partial^2 u^{(e)}}{\partial y^2} - \frac{1}{4} \frac{\partial u^{(e)}}{\partial t} + A \frac{\partial u^{(e)}}{\partial y} - R u^{(e)} + P \right] \right\} dy = 0$$

Where
$$N^T = \begin{bmatrix} N_j & N_k \end{bmatrix}^T = \begin{bmatrix} N_j \\ N_k \end{bmatrix}$$
, $A = 1 + \varepsilon e^{int}$, $R = \frac{1}{K_o A} + M^2$, $P = GrT + GmC$

Let the linear piecewise approximation solution

$$u^{(e)} = N_{j}(y)u_{j}(t) + N_{k}(y)u_{k}(t) = N_{j}u_{j} + N_{k}u_{k}$$

The element equation is given by

$$\int_{y_{j}}^{y_{k}} \left\{ \begin{bmatrix} N_{j}^{'} N_{j}^{'} & N_{j}^{'} N_{k}^{'} \\ N_{j}^{'} N_{k}^{'} & N_{k}^{'} N_{k}^{'} \end{bmatrix} \begin{bmatrix} u_{j} \\ u_{k} \end{bmatrix} \right\} dy + \frac{1}{4} \int_{y_{j}}^{y_{k}} \left\{ \begin{bmatrix} N_{j} N_{j} & N_{j} N_{k} \\ N_{j} N_{k} & N_{k} N_{k} \end{bmatrix} \begin{bmatrix} \cdot \\ u_{j} \\ \cdot \\ u_{k} \end{bmatrix} \right\} dy - A \int_{y_{j}}^{y_{k}} \left\{ \begin{bmatrix} N_{j} N_{j}^{'} & N_{j} N_{k} \\ N_{j}^{'} N_{k} & N_{k}^{'} N_{k} \end{bmatrix} \begin{bmatrix} u_{j} \\ u_{k} \end{bmatrix} \right\} dy$$

$$+\mathbf{R}\int_{y_{j}}^{y_{k}}\left\{\begin{bmatrix}N_{j} N_{j} & N_{j} N_{k}\\N_{j} N_{k} & N_{k} N_{k}\end{bmatrix}\begin{bmatrix}u_{j}\\u_{k}\end{bmatrix}\right\}dy - \mathbf{P}\int_{y_{j}}^{y_{k}}\begin{bmatrix}N_{j}\\N_{k}\end{bmatrix}dy = 0$$

Where prime and dot denotes differentiation w.r.to 'y' and 't ' respectively. Simplifying we get

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$$\frac{1}{l^{(e)^2}} \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} u_j \\ u_k \end{bmatrix} + \frac{1}{24} \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix} \begin{bmatrix} \bullet \\ u_j \\ \bullet \\ u_k \end{bmatrix} - \frac{A}{2l^{(e)}} \begin{bmatrix} -1 & 1 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} u_j \\ u_k \end{bmatrix} + \frac{R}{6} \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix} \begin{bmatrix} u_j \\ u_k \end{bmatrix} = \frac{P}{2} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

Where $l^{(e)} = y_k - y_j = h$

In order to get the differential equation at the knot x_i , we write the element equations for the elements $y_{i+1 \le} y \le y_i$ and $y_i \le y \le y_{i+1}$ assemble two element equations, we obtain

$$\frac{1}{l^{(e)^2}} \begin{bmatrix} 1 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 1 \end{bmatrix} \begin{bmatrix} u_{i-1} \\ u_i \\ u_{i+1} \end{bmatrix} + \frac{1}{24} \begin{bmatrix} 2 & 1 & 0 \\ 1 & 4 & 1 \\ 0 & 1 & 2 \end{bmatrix} \begin{bmatrix} \cdot \\ u_i \\ \cdot \\ u_{i+1} \end{bmatrix} - \frac{A}{2l^{(e)}} \begin{bmatrix} -1 & 1 & 0 \\ -1 & 0 & 1 \\ 0 & -1 & 1 \end{bmatrix} \begin{bmatrix} u_{i-1} \\ u_i \\ u_{i+1} \end{bmatrix} + \frac{R}{6} \begin{bmatrix} 2 & 1 & 0 \\ 1 & 4 & 1 \\ 0 & 1 & 2 \end{bmatrix} \begin{bmatrix} u_{i-1} \\ u_i \\ u_{i+1} \end{bmatrix} = \frac{P}{2} \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}$$

We put the row equation corresponding to the knot 'i', is

$$\frac{1}{l^{(e)^2}} \left[-u_{i-1} + 2u_i - u_{i+1} \right] + \frac{1}{24} \left[\overset{\bullet}{u_{i-1}} + \overset{\bullet}{4u_i} + \overset{\bullet}{u_{i+1}} \right] - \frac{A}{2l^{(e)}} \left[-u_{i-1} + u_{i+1} \right] + \frac{R}{6} \left[u_{i-1} + 4u_i + u_{i+1} \right] = P$$
(5)

Applying Crank-Nicholson method to the above equation (5), then we gets

$$A_{1}u_{i-1}^{n+1} + A_{2}u_{i}^{n+1} + A_{3}u_{i+1}^{n+1} = B_{1}u_{i-1}^{n} + B_{2}u_{i}^{n} + B_{3}u_{i+1}^{n} + P^{*}$$
(6)

Where $A_1 = 1 + 2Rk - 12r + 6Arh$; $A_2 = 4 + 24r + 8Rk$; $A_3 = 1 + 2Rk - 12r - 6Arh$; $1 - 2Pk + 12r - 6\Delta rh; \quad R_2 - 4 - 24r - 8Rk; \quad R_3 = 1 - 2Rk + 12r + 6Arh;$

$$B_1 = 1 - 2Rk + 12r - 6Arh; B_2 = 4 - 24r - 8Rk; B_3 = 1 - 2Rk + 12r + 6Arh;$$

$$P^* = 24(Gr)kT_i^j + 24(Gm)kC_i^j;$$

Applying similar procedure to equation (2), then we gets

$$G_1 T_{i-1}^{n+1} + G_2 T_i^{n+1} + G_3 T_{i+1}^{n+1} = H_1 T_{i-1}^n + H_2 T_i^n + H_3 T_{i+1}^n + Q^*$$
(7)

Where $G_1 = Pr + 6Arh(Pr) - 12r$; $G_2 = 4Pr + 24r$; $G_3 = Pr - 6Arh(Pr) - 12r$;

 $H_1 = Pr - 6Arh(Pr) + 12r; H_2 = 4Pr - 24r; H_3 = Pr + 6Arh(Pr) + 12r;$

$$Q^* = 24k(\Pr)Du\left(\frac{\partial^2 C}{\partial y^2}\right);$$

Applying similar procedure to equation (3), then we gets

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$$J_1 C_{i-1}^{n+1} + J_2 C_i^{n+1} + J_3 C_{i+1}^{n+1} = I_1 C_{i-1}^n + I_2 C_i^n + I_3 C_{i+1}^n + B^*$$
(8)

Where $J_1 = Sc + 6Arh(Sc) - 12r$; $J_2 = 4Sc + 24r$; $J_3 = Sc - 6Arh(Sc) - 12r$;

$$I_1 = Sc - 6Arh(Sc) + 12r; I_2 = 4Sc - 24r; \qquad I_3 = Sc + 6Arh(Sc) + 12r;$$
$$B^* = 24k(Sc)So\left(\frac{\partial^2 T}{\partial y^2}\right);$$

Here $r = \frac{k}{L^2}$ and k, h are mesh sizes along y- direction and time-direction respectively index

'i' refers to space and j refers to time. The mesh system consists of h=0.1 and k=0.01. In the equations (6), (7) and (8), taking i = 1(1)10 and using boundary conditions in (4), then we

get the following tri-diagonal system of equations

$$Au = B \tag{9}$$

$$ET = F \tag{10}$$

$$XC = Y \tag{11}$$

Where A, E and X are the tri-diagonal matrices of order ten and whose elements are defined by

$$A_{i,i} = A_2; E_{i,i} = G_2; X_{i,i} = J_2;$$
 at $i = 1(1) n$

$$\begin{split} A_{i\text{-}1,i} &= A_1; E_{i\text{-}1,i} = G_1; \quad X_{i\text{-}1,i} = J_1; \qquad \qquad \text{at } i = 2(1) \text{ n} \\ A_{i,i+1} &= A_3; E_{i,i+1} = G_3; \quad X_{i,i+1} = J_3; \qquad \qquad \text{at } i = 2(1) \text{ n} \end{split}$$

And u, B, T, F, C, Y are column matrices having n-components, which are column matrices having components namely $u_{i,j+1}$, B(i,j), $T_{i,j+1}$, F(i,j), $C_{i,j+1}$ and Y(i,j); i=1(1)10 respectively. The solutions of (9), (10) and (11) can be obtained by Thomas algorithm. To judge the accuracy of convergence and stability of finite element method, the programmed was run with smaller values of k. i.e. k=0.005 and no significant change was observed. Hence we conclude that the finite element method is stable and convergent.

SKIN-FRICTION, RATE OF HEAT AND MASS TRANSFER:

Skin-Friction co-efficient (τ) at the plate is $\tau = \left(\frac{\partial u}{\partial y}\right)_{y=0}$

Heat transfer co-efficient (N_u) at the plate is $N_u = -\left(\frac{\partial\theta}{\partial y}\right)_{y=0}$

Mass transfer co-efficient (S_b) at the plate is $S_b = -\left(\frac{\partial C}{\partial y}\right)_{y=0}$

RESULTS AND DISCUSSIONS:

In order to get a physical view of the problem, numerical calculations have been carried out for the non-dimensional velocity (u), temperature (T), concentration (C), skin-friction coefficient (τ) and heat and mass transfer coefficients in terms of Nusselt number (Nu) and Sherwood number (Sh) for different flow parameters. The effects of material parameters such as Prandtl number (Pr), Schmidt number (Sc), magnetic parameter (M), permeability parameter (Ko), Soret number or Thermal Diffusion (So), Dufour number or Diffusion Thermo (Du), Grashof number (Gr) and modified Grashof number (Gm) have been observed numerically. The numerical calculations of these results are presented graphically in Figs 1 to 14. During the course of numerical calculations of the velocity, temperature and concentration, the values of the Prandtl number are chosen for air (Pr = 0.71), electrolytic solution (Pr = 1.0), water (Pr = 7.0) and water at 4°C (Pr = 11.40). To focus out attention on numerical values of the results obtained in the study the values of Sc are chosen for the gases representing diffusing chemical species of most common interest in air namely Hydrogen (Sc = 0.22), Water-vapour (Sc = 0.60), Oxygen (Sc = 0.66), Methanol (Sc = 1.00) and Propyl-benzene (Sc = 2.62) at 20°C and one atmospheric pressure. For the physical significance, only the real part of complex quantity is invoked for the numerical discussion in the problem and at t=1.0, stable values for velocity, temperature and concentration fields are obtained. To examine the effect of parameters related to the problem on the velocity field and skin-friction numerical computations are carried out at (Pr = 0.71) which corresponds to air at 25°C and one atmospheric pressure. The values of Grashof number Gr and modified Grashof number Gm are taken to be positive and negative as they respectively represent symmetric cooling of the channel walls when Gr > 0 and symmetric heating of the channel walls when Gr < 0.

The temperature and the species concentration are coupled to the velocity via Grashof number Gr and modified Grashof number Gm as seen in equation (1). Figures 1 - 6 display the effects of material parameters such as Gr, Gm, M, Du, So and Ko on the velocity field for both externally cooling (Gr > 0) and heating (Gr < 0) of the plate. It is observed that an increase in the Grashof number or modified Grashof number leads to increase in the velocity field in both the presence of cooling and heating of the plate. A comparison of velocity field curves due to cooling of the plate shows that the velocity increases rapidly near the plate and after attaining a maximum value, it decreases as y increases.

The effect of Magnetic field parameter M is shown in the figure 5 in case of cooling of the plate. It is observed that the velocity of the fluid decreases with the increase of Magnetic parameter values. We also see that velocity profiles decrease with the increase of magnetic effect indicating that magnetic field tends to retard the motion of the fluid. Magnetic field may control the flow characteristics.

Figures (3) and (4) show the effects of Dufour number Du and Soret number So on velocity field u. From these figures, it is observed that the velocity u increases as Dufour number Du and Soret number So increases in case of cooling of the plate. It is interesting note that the effect of Dufour and Soret numbers on velocity field are significant. This is because either a decrease in concentration difference or an increase in temperature difference leads to an increase in the value of the Soret parameter (So). Hence increasing the Soret parameter (So) increases the velocity of the fluid. Figure (6) exhibits the effect of Ko on velocity field u.

From this figure, it is observed that an increase in Ko increases the velocity u in case of cooling of the plate. In the figures (3) - (6) on velocity field mentioned above, compare to the case of cooling of the plate opposite effects are observed in the case of heating of the plate.

In figure (7) we depict the effect of Prandtl number Pr on the temperature field. It is observed that an increase in the Prandtl number leads to decrease in the temperature field. Also, temperature field falls more rapidly for water in comparison to air and the temperature curve is exactly linear for mercury, which is more sensible towards change in temperature. From this observation it is conclude that mercury is most effective for maintaining temperature differences and can be used efficiently in the laboratory. Air can replace mercury, the effectiveness of maintaining temperature changes are much less than mercury. However, air can be better and cheap replacement for industrial purpose. This is because, either increase of kinematic viscosity or decrease of thermal conductivity leads to increase in the value of Prandtl number Pr. Hence temperature decrease with the increasing of Prandtl number Pr. Figure (8) depicts the effects of the Dufour number on the fluid temperature. It can be clearly seen from this figure that diffusion thermal effects greatly affect the fluid temperature also increases.

The effects of Schmidt number Sc and Soret number So on the concentration field are presented in figures (9) and (10). Fig. 9 shows the concentration field due to variation in Schmidt number Sc for the gasses Hydrogen, Water-vapour, Oxygen and Methanol. It is observed that concentration field is steadily for Hydrogen and falls rapidly for Oxygen and Methanol in comparison to Water-vapour. Thus Hydrogen can be used for maintaining effective concentration field and Water-vapour can be used for maintaining normal concentration field. In the figure (10), it is observed that an increase in the Soret number leads to increase in the concentration field.

The variation of Skin-friction, Nusselt number and Sherwood number with different flow parameters shown in graphically in figure (11) to (14).

Table -1 presents numerical values of the skin-friction coefficient (τ) for variations in Gr, Gm, M, Ko, Pr, Sc, So and Du for externally cooling of the plate (Gr > 0). It is observed that, an increase in the Prandtl number or Schmidt number or magnetic parameter leads to

decrease in the value of skin-friction coefficient while an increase in the permeability parameter or Soret number or Dufour number or Grashof number or modified Grashof number leads to increase in the value of skin-friction coefficient.

Table - 2 presents numerical values of the skin-friction coefficient (τ) for variations in Gr, Gm, M, Ko, Pr, Sc, So and Du for externally heating of the plate (Gr < 0). It is observed that, an increase in the Schmidt number or permeability parameter or Dufour number leads to decrease in the value of skin-friction coefficient while an increase in the Prandtl number or magnetic parameter or Soret number or Grashof number or modified Grashof number leads to increase in the value of skin-friction coefficient.

Table - 3 presents numerical values of heat transfer coefficient in terms of Nusselt number (Nu) for different values of the Prandtl number Pr and Dufour number Du respectively. It is observed that an increase in the Dufour number leads to decrease in the value of heat transfer coefficient while an increase in the Prandtl number leads to decrease in the value of heat transfer coefficient.

Table - 4 presents numerical values of mass transfer coefficient in terms of Sherwood number (S_b) for different values of Schmidt number Sc and Soret number So respectively. It is observed that an increase in the Schmidt number leads to decrease in the value of mass transfer coefficient while an increase in the Soret number leads to increase in the value of mass transfer coefficient.

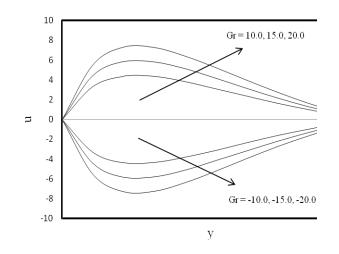


Figure 1. Effect of Heat transfer 'Gr' on Velocity field 'u' for cooling (Gm = 5.0) and heating of the plate (Gm = -5.0).

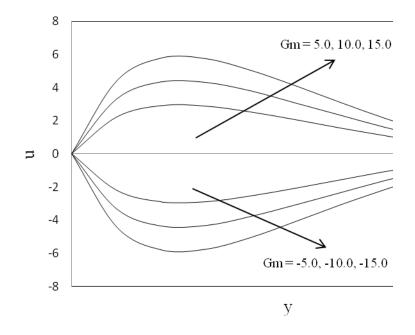


Figure 2. Effect of Mass transfer 'Gm' on Velocity field 'u' for cooling (Gr = 5.0) and heating of the plate (Gr = -5.0).

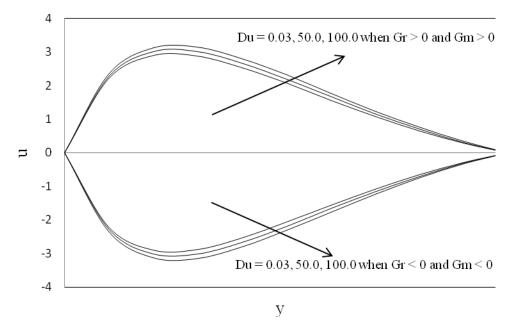
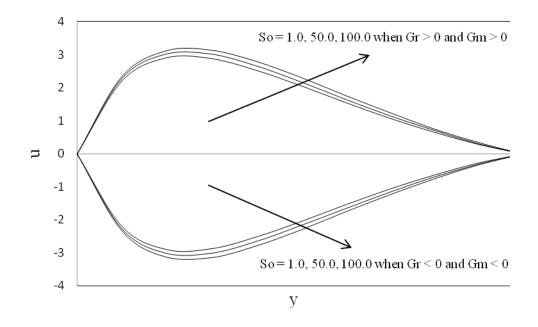


Figure 3. Effect of Dofour number 'Du' on Velocity field 'u' for cooling (Gr = 5.0 & Gm = 5.0) and heating of the plate (Gr = -5.0 & Gm = -5.0).



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Figure 4. Effect of Soret number 'So' on Velocity field 'u' for cooling (Gr = 5.0 & Gm = 5.0) and heating of the plate (Gr = -5.0 & Gm = -5.0).

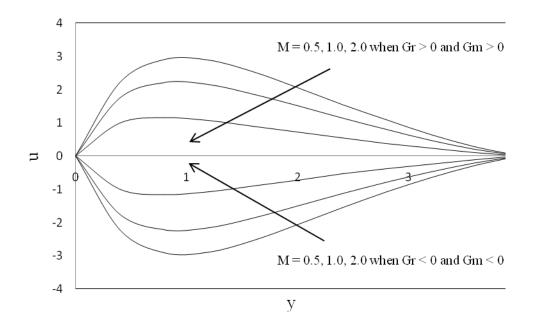


Figure 5. Effect of Magnetic parameter 'M' on Velocity field 'u' for cooling (Gr = 5.0 & Gm = 5.0) and heating of the plate (Gr = -5.0 & Gm = -5.0).

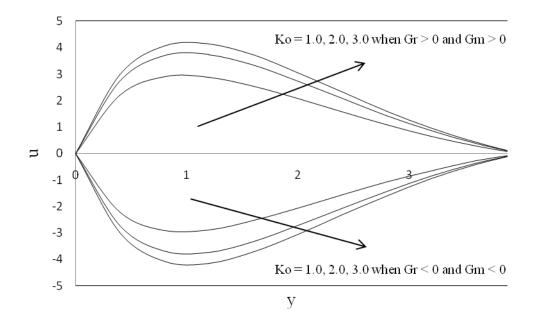


Figure 6. Effect of Permeability parameter 'Ko' on Velocity field 'u' for cooling (Gr = 5.0 & Gm = 5.0) and heating of the plate (Gr = -5.0 & Gm = -5.0).

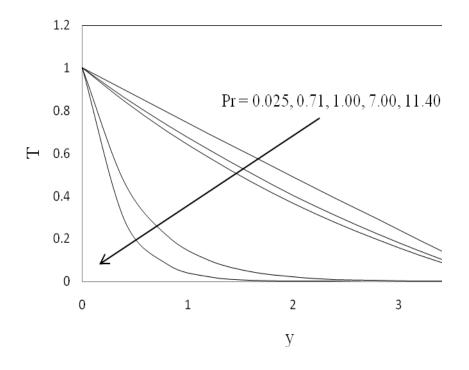


Figure 7. Effect of Prandtl number 'Pr' on Temperature field 'T'.

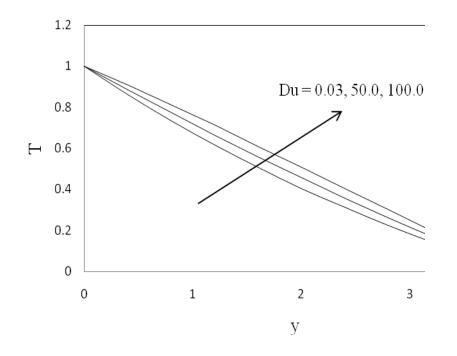


Figure 8. Effect of Dufour number 'Du' on Temperature field 'T'.

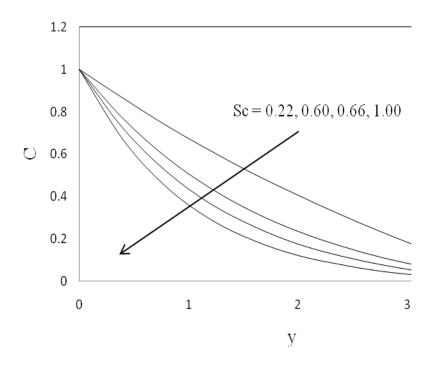


Figure 9. Effect of Schmidt number 'Sc' on Concentration field 'C'.

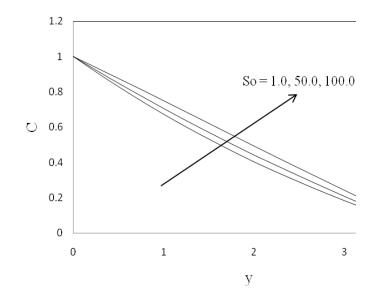


Figure 10. Effect of Soret number 'So' on Concentration field 'C' .

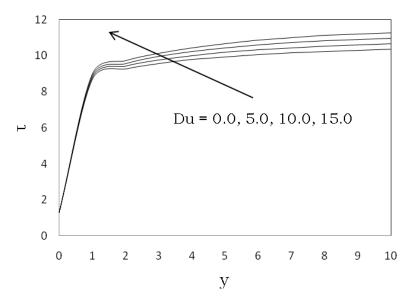


Figure 11. The variation of skin-friction with increasing Dufour number with Gr = Gm = 1.0, M = 1.0, m = 1.0, Pr = 0.71, Sc = 0.22, So = 0.0.

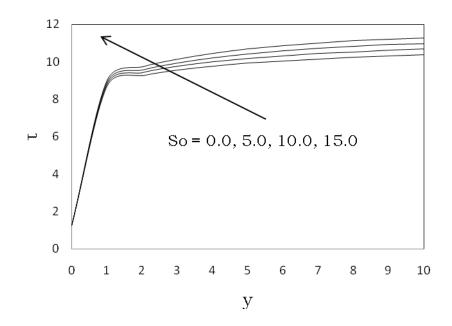


Figure 12. The variation of skin-friction with increasing Soret number with Gr = Gm = 1.0, M = 1.0, m = 1.0, Pr = 0.71, Sc = 0.22, Du = 0.0.

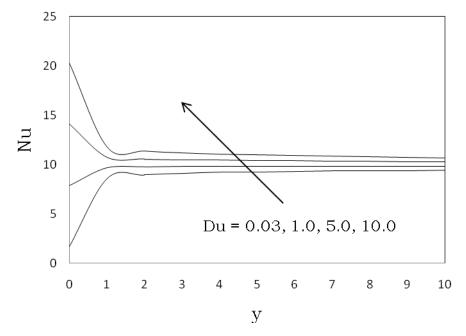


Figure 13. The variation of Nusselt number with increasing Dufour number with Gr = Gm =1.0, M = 1.0, m = 1.0, Pr = 0.71, Sc = 0.22, So = 0.0.

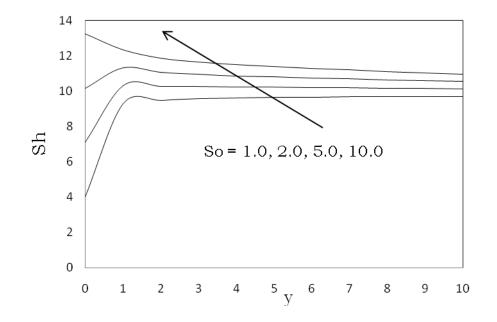


Figure 14. The variation of Sherwood number with increasing Soret number with Gr = Gm = 1.0, M = 1.0, m = 1.0, Pr = 0.71, Sc = 0.22, Du = 0.0.

Table 1

Skin-friction coefficient (τ) for cooling of the plate

Gr	Gm	М	Ko	Pr	Sc	So	Du	7
GI	GIII	IVI	KO	F 1	30	30	Du	τ
5.0	5.0	0.5	1.0	0.71	0.22	1.0	0.03	7.6014
10.0	5.0	0.5	1.0	0.71	0.22	1.0	0.03	11.4250
5.0	10.0	0.5	1.0	0.71	0.22	1.0	0.03	11.3793
5.0	5.0	1.0	1.0	0.71	0.22	1.0	0.03	6.1951
5.0	5.0	0.5	2.0	0.71	0.22	1.0	0.03	9.1764
5.0	5.0	0.5	1.0	7.0	0.22	1.0	0.03	5.3787
5.0	5.0	0.5	1.0	0.71	0.60	1.0	0.03	6.9138
5.0	5.0	0.5	1.0	0.71	0.22	2.0	0.03	7.6054
5.0	5.0	0.5	1.0	0.71	0.22	1.0	1.0	7.6052

Gr	Gm	М	Ko	Pr	Sc	So	Du	τ
-5.0	5.0	0.5	1.0	0.71	0.22	1.0	0.03	-0.0456
-10.0	5.0	0.5	1.0	0.71	0.22	1.0	0.03	-3.8692
-5.0	10.0	0.5	1.0	0.71	0.22	1.0	0.03	3.7323
-5.0	5.0	1.0	1.0	0.71	0.22	1.0	0.03	-0.0324
-5.0	5.0	0.5	2.0	0.71	0.22	1.0	0.03	-0.0619
-5.0	5.0	0.5	1.0	7.0	0.22	1.0	0.03	2.2237
-5.0	5.0	0.5	1.0	0.71	0.60	1.0	0.03	-0.7337
-5.0	5.0	0.5	1.0	0.71	0.22	2.0	0.03	-0.0416
-5.0	5.0	0.5	1.0	0.71	0.22	1.0	1.0	-0.0495

Table 2 Skin-friction coef	fficient (τ) for	heating of the plate

Table 3

Heat transfer coefficient in terms of Nusselt number

Pr	Du	Nu
0.71	0.03	9.6443
7.00	0.03	8.2569
0.71	1.0	9.6456

Table 4

Mass transfer coefficient in terms of Sherwood number

Sc	So	S _b
0.22	1.0	9.6295
0.60	1.0	9.3635
0.22	2.0	9.6308

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